## Abington Heights School District Algebra II Accelerated Curriculum



In Algebra II Accelerated, students develop their numeracy skills through the following areas of study:

1. Patterns, Relations, and Functions
2. Applications of Functions
3. Operations with Complex Numbers
4. Non-Linear Expressions
5. Non-Linear Equations
6. Data Analysis

Board Approval Date: June 7, 2023
Adoption: 2023-2024 SY
Review Date:


## Abington Heights Math Framework

| Stakeholders | Actions |
| :---: | :---: |
| Students | ڤ Engage in mathematical discussions, share their ideas openly, be inquisitive, seek to understand and learn more about mathematical concepts, and try their best daily. <br> ฝ Exhibit creativity and curiosity in problem solving individually and collaboratively. <br> $\star$ Persevere in engaging and challenging daily mathematical practice. <br> $\star$ Come prepared to learn every day. |
| Teachers | $\star$ Create a safe and collaborative classroom environment where students feel vested in a shared vision for mathematical excellence. <br> $\star$ Develop high quality instruction that meets the needs of all learners through differentiation. <br> $\star$ Use a variety of 21st century methodologies to advance learning. <br> $\star$ Partner with parents and guardians to support student success. <br> $\star$ Establish a collaborative community within the building and amongst grade levels to ensure a cohesive level of instruction. |
| Building Leaders | $\star$ Deeply understand the needs of teachers, students, the instructional materials being used, programs being implemented, and the expectations for state-level assessment scores <br> - Knowledgeable about program and grade level standards <br> - Ensure consistent and equal access to high-quality instructional materials and resources, building. <br> $\star$ Be partners with teachers, students and families: <br> - Provide guidance and support to the mathematical community. <br> - Understand needs of teachers, students and families. <br> $\star$ Trust the educators to make professional decisions based on program, student, and district needs. |
| Central Admin | $\star$ Effectively communicate to the school board and community specific areas of need and how to support teachers and building leaders in a quest for mathematical excellence <br> $\star$ Deeply understand the needs of teachers, students, the instructional materials being used, programs being implemented, and the expectations for state-level assessment scores <br> - Have a common metric for mathematical excellence. <br> - Ensure consistent and equal access to high-quality instructional materials and resources, district. <br> - Re-examine best practices/curriculum routinely ( 6 years). <br> $\star$ Support a culture of collaboration between the other stakeholder groups to maintain the standard of excellence of the Abington Heights <br> $\star$ Trust the educators to make professional decisions based on program, student, and district needs. |
| Parents/ Community | $\star$ Be a strong support system and contribute by building a positive math community for students. <br> $\star$ Encourage a positive math mindset. <br> $\star$ Have conversations with their children about school and ask what they are learning about in school. <br> $\star$ Be open, receptive to the district's ideas about student learning and reach out to teachers/school to learn more about how they can support. <br> $\star$ Trust the educators to make professional decisions based on program, student, and district needs. |
| School Board | $\star$ Provide the fiscal resources to support: <br> - Highly qualified professionals for mathematics <br> - High-quality instructional materials <br> - Effective and efficient math interventions for remediation <br> - Professional development for math content and instructional practices <br> Trust the educators to make professional decisions based on program, student, and district needs. |

Algebra II Accelerated Scope and Sequence

| Month | Unit | Estimated Number of Weeks |
| :--- | :--- | :---: |
| September | Essentials of Algebra I | 4 |
| October | Essentials of Algebra I | 2 |
|  | $\mathrm{f}(\mathrm{x})$ Notation \& Special Functions | 2 |
| November | $\mathrm{f}(\mathrm{x})$ Notation \& Special Functions | 2 |
|  | Quadratic Functions | 2 |
|  | Quadratic Functions | 2 |
| January | Quadratic Functions | 2 |
|  | Radical Expressions \& Complex <br> Numbers | 2 |
| February | Radical Expressions \& Complex <br> Numbers | 2 |
|  | Rational Equations \& Functions | 2 |
| March | Polynomial Functions | 4 |
| April | Polynomial Functions | 1 |
|  | Exponential and Logarithmic <br> Functions | 3 |
| May Exponential and Logarithmic <br> Functions <br>  Conic Sections | 2 |  |
|  | Probability | 1 |


| Unit | Essential Questions | Content | Skills | PA Core Standards | Activities | Assessment/ Evidence of Learning |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Essentials of Algebra I | How do I simplify algebraic expressions? <br> What are the order of operations? <br> How do I use the inverse order of operations to solve equations? <br> How do I solve absolute value equations and inequalities? <br> How do the solution methods and the solutions of linear equations and inequalities in one variable compare? | Real number operations <br> Algebraic expressions and models <br> Solving equations <br> Solving literal equations <br> Absolute value equations and inequalities <br> Inequalities <br> Interval Notation | Simplify and evaluate expressions using order of operations <br> Solve multi-step equations in one variable <br> Use algebraic processes to solve a formula for a given variable <br> Solve absolute value equations and inequalities in one variable <br> Solve inequalities in one variable, expressing solution in interval notation and graph solution on number line | CC.2.1.HS.F. 5 CC.2.2.HS.D. 7 CC.2.2.HS.C. 1 CC.2.2.HS.C. 2 CC.2.2.HS.C. 3 CC.2.2.HS.C. 6 CC.2.2.HS.D. 10 | First day of school activity - review of order of operations <br> Delta Math/Webwork <br> Class <br> Participation <br> Discovery <br> Activities <br> Flipcharts/Google Slides | Webwork/Delta Math <br> Homework Assignments <br> Quizzes |


| Unit | Essential Questions | Content | Skills | PA Core <br> Standards | Activities | Assessment/ Evidence of Learning |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Essentials of Algebra I (continued) | What is a function? <br> How can I determine the domain \& range of a function using a graph, table, or an equation? | Relations and Functions <br> Domain and Range Interval Notation Evaluate functions | Determine if a relation is a function <br> Find the domain and range of a relation or function in interval notation <br> Evaluate a function at a given value |  |  |  |
|  | How do I find the equation given basic information about a line? <br> How can I manipulate a linear equation to be in the three different forms? <br> How can I determine a perpendicular or parallel relationship of a line? | Slope and rate of change <br> Equations of lines <br> Regression equations (lines of best fit) | Calculate slope <br> Write equations of lines when given various pieces of information (slope and point, two points, parallel / perpendicular relationship) in point-slope, slope-intercept, or standard form <br> Make predictions using the equations or graphs of regression models (lines of best fit) of scatter plots. |  |  |  |


| Unit | Essential Questions | Content | Skills | PA Core Standards | Activities | Assessment/ Evidence of Learning |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Essentials of Algebra I (continued) | How can I manipulate equations to solve a system of equations? <br> What is the difference between solving systems of equations by elimination \& substitution methods? <br> How do I know where to shade when graphing systems of inequalities? | $\overline{\text { Systems of linear }}$ equations in two variables <br> Systems of linear inequalities in two variables | Solve systems of linear equations in two variables by graphing <br> Solve systems of linear equations in two variables by elimination <br> Solve systems of linear equations in two variables by substitution <br> Solve systems of linear inequalities in two variables by graphing |  |  |  |
| $\mathrm{f}(\mathrm{x})$ Notation \& Special Functions | How do I use $f(x)$ notation to determine the value of the function using a graph? <br> How do I use f(x) notation to determine the value of the function using an equation? | $f(x)$ notation <br> Operations with $\mathrm{f}(\mathrm{x})$ Notation <br> Combination of Functions <br> Absolute Value Equations <br> Piecewise Functions | Finding function value from a graph, table, or equation <br> Add, subtract, multiply, divide with $f(x)$ notation <br> Graph transformations of absolute value functions | CC.2.1.HS.F. 3 | Delta <br> Math/Webwork <br> Class <br> Participation <br> Discovery <br> Activities <br> Flipcharts/Google Slides | Webwork/Delta Math <br> Homework Assignments <br> Quizzes <br> Special Functions \& $\mathrm{f}(\mathrm{x})$ Notation Test |


| Unit | Essential Questions | Content | Skills | PA Core Standards | Activities | Assessment/ Evidence of Learning |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{f}(\mathrm{x})$ Notation \& Special Functions (continued) | How do I use f(x) notation to determine the combination of functions? | Step Functions | Graph piecewise functions with an input-output table <br> Use step functions to model real world applications |  |  |  |
| Quadratic Functions | How do I solve quadratic equations? <br> What are the elements of a parabola? <br> How do I determine which method to use for factoring? | Factoring <br> Solving using square roots <br> Complex numbers <br> Quadratic <br> Formula <br> Discriminant <br> Quadratic inequalities <br> Modeling quadratic functions | Solve quadratic equations by factoring, taking square roots, and using quadratic formula <br> Utilize the discriminant to determine \# of real zeros <br> Use the graphing calculator to find points of interest (vertex, zeros, y-intercepts, values of intersection, etc.) <br> State domain and range | CC.2.1.HS.F. 3 CC.2.1.HS.F. 4 CC.2.1.HS.F. 6 CC.2.1.HS.F. 7 CC.2.2.HS.D. 5 CC.2.2.HS.D. 6 CC.2.2.HS.D. 7 CC.2.2.HS.D. 8 CC.2.2.HS.D. 9 CC.2.2.HS.D. 10 CC.2.2.HS.C. 3 CC.2.2.HS.C. 4 CC.2.2.HS.C. 5 | Delta <br> Math/Webwork <br> Class <br> Participation <br> Discovery <br> Activities <br> Flipcharts/Google Slides | Webwork/Delta Math <br> Homework Assignments <br> Quizzes <br> Chapter 5 Test |


| Unit | Essential Questions | Content | Skills | PA Core Standards | Activities | Assessment/ Evidence of Learning |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Radical Expressions \& Complex Numbers | What is a complex number? <br> How can I use properties of radicals to simplify an expression? | Properties of Radicals Operations with Radicals <br> Rationalizing the Denominator <br> Complex Numbers | Use properties of radicals to simplify expressions <br> Add, subtract, multiply \& divide with radicals <br> Using properties of radicals to rationalize the denominator <br> Operations with complex numbers <br> Solve radical equations | CC.2.1.HS.F. 1 CC.2.1.HS.F. 6 CC.2.1.HS.F. 7 CC.2.2.HS.D. 5 CC.2.2.HS.D. 6 CC.2.2.HS.D. 7 CC.2.2.HS.D. 8 CC.2.2.HS.D. 9 CC.2.2.HS.D. 10 CC.2.2.HS.C. 3 | Delta <br> Math/Webwork <br> Class <br> Participation <br> Discovery <br> Activities <br> Flipcharts/Google Slides | Webwork/Delta Math <br> Homework Assignments <br> Radicals Quiz <br> Test |
| Rational Equations \& Functions | How can I determine the LCD of a rational equation? <br> How can I use factoring to simplify rational functions? | Operations with rational functions <br> Simplifying <br> Rational <br> Functions <br> Complex <br> Fractions | Using Common factors to simplify a rational expression <br> Multiply \& Dividing Rational Functions using common factors <br> Adding and subtracting rational functions using least common denominator | CC.2.2.HS.D. 1 CC.2.2.HS.D. 2 CC.2.2.HS.D. 3 CC.2.2.HS.D. 4 CC.2.2.HS.D. 5 CC.2.2.HS.D. 6 CC.2.2.HS.D. 7 CC.2.2.HS.D. 8 | Delta <br> Math/Webwork <br> Class <br> Participation <br> Discovery <br> Activities <br> Flipcharts/Google Slides | Webwork/Delta Math <br> Homework Assignments <br> Quizzes <br> Test |


| Unit | Essential Questions | Content | Skills | PA Core Standards | Activities | Assessment/ Evidence of Learning |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Rational Equations \& Functions (continued) |  |  | Solve rational equations | CC.2.2.HS.D. 9 CC.2.2.HS.D. 10 |  |  |
| Polynomial Functions | How can I find the zeros of a polynomial function algebraically / graphically? <br> What are the exponent properties? And how can I use them to simplify? | Properties of exponents <br> Evaluating and graphing polynomial functions <br> Adding, subtracting, multiplying and dividing polynomials <br> Factoring and solving polynomial equations <br> Remainder and factor theorem <br> Finding rational zeros <br> Analyze graphs of polynomial functions <br> Model with poly. functions | Simplify expressions using exponent rules <br> Complete polynomial operations <br> Graph polynomial functions <br> Use the graphing calculator to find points of interest (local min/max, zeros, y-intercepts, values of intersection, etc.) <br> Find zeros (algebraically and graphically) <br> State domain and range | CC.2.1.HS.F. 3 CC.2.2.HS.D. 1 CC.2.2.HS.D. 2 CC.2.2.HS.D. 3 CC.2.2.HS.D. 4 CC.2.2.HS.D. 5 CC.2.2.HS.D. 7 CC.2.2.HS.C. 1 CC.2.2.HS.C. 2 CC.2.2.HS.C. 3 CC.2.2.HS.C. 5 CC.2.2.HS.C. 6 | Delta <br> Math/Webwork <br> Class <br> Participation <br> Discovery <br> Activities <br> Flipcharts/Google <br> Slides | Webwork/Delta Math <br> Homework Assignments <br> Quizzes <br> Test |


| Unit | Essential Questions | Content | Skills | PA Core Standards | Activities | Assessment/ Evidence of Learning |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Exponential and Logarithmic Functions | What does it mean to be exponential? <br> What is a logarithm? <br> What are the properties of logarithms? <br> What is the relationship between logarithms and exponential functions? <br> Can I solve logarithmic and exponential equations? | Exponential functions <br> The number $e$ <br> Inverse functions <br> Logarithmic functions <br> Properties of logarithms <br> Solving exponential and logarithmic equations <br> Natural logarithms | Use logarithmic properties to simplify <br> expressions <br> Condense and expand logarithms <br> Graph exponential and logarithmic equations <br> Solve exponential and logarithmic equations | CC.2.1.HS.F. 1 CC.2.2.HS.D. 2 CC.2.2.HS.D. 5 CC.2.2.HS.D. 7 CC.2.2.HS.D. 8 CC.2.2.HS.D. 9 CC.2.2.HS.D. 10 CC.2.2.HS.C. 2 CC.2.2.HS.C. 3 CC.2.2.HS.C. 4 CC.2.2.HS.C. 5 CC.2.2.HS.C. 6 | Delta <br> Math/Webwork <br> Class <br> Participation <br> Discovery <br> Activities <br> Flipcharts/Google Slides | Webwork/Delta Math <br> Homework Assignments <br> Quizzes <br> Test |
| Conic Sections | What are the conic sections? <br> How can I determine the conics from equations and graphs? | Parabolas <br> Circles <br> Ellipses <br> Hyperbolas <br> Identifying conic sections | Write and graph equations of circles <br> Using characteristics to identify conics | CC.2.3.HS.A. 10 | Delta <br> Math/Webwork <br> Class <br> Participation <br> Discovery <br> Activities <br> Flipcharts/Google Slides | Webwork/Delta Math <br> Homework Assignments <br> Quiz |


| Unit | Essential Questions | Content | Skills | PA Core Standards | Activities | Assessment/ Evidence of Learning |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Probability | How can you find the probability of events and combinations of events? <br> How are conditional probability and independence related? <br> How are combinations and permutations useful when finding probabilities? <br> How are odds and probabilities related? | Probability <br> Odds <br> Combinations <br> Permutations <br> Fundamental Counting Principle <br> Independent, Dependent, and Compound Events | Use <br> combinations, permutations, and the fundamental counting principle to solve problems involving probability <br> Use odds to find probability and/or use probability to find odds <br> Use probability for independent, dependent, or compound events to predict outcomes | CC.2.4.HS.B. 4 CC.2.4.HS.B. 5 CC.2.4.HS.B. 6 CC.2.4.HS.B. 7 | Delta <br> Math/Webwork <br> Class <br> Participation <br> Discovery <br> Activities <br> Flipcharts/Google Slides | Webwork/Delta Math <br> Homework Assignments <br> Quiz |

## Portrait of an Abington Heights Mathematician

By the end of Algebra II, students will:

| Patterns, Relations, and Functions | Applications of Functions | Operations with Complex Numbers | Non-Linear Expressions | Non-Linear Equations | Data Analysis |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Analyze a set of data for the existence of a pattern, and represent the pattern with a rule algebraically and/or graphically Determine the domain, range, or inverse of a relation Identify and/or determine the characteristics of an exponential, quadratic, or polynomial function (e.g. intercepts, zeros) | Create, interpret, and/or use the equation, graph, or table of quadratic, absolute value, piecewise, and step functions Determine, use, and/or interpret minimum and maximum values over a specified interval of a graph of quadratic, absolute value, piecewise, or step functions Translate a quadratic, absolute value, piecewise, and step function from one representation of a function to another (graph, table, and equation) | Simplify/write square roots in terms of $i$ Simplify/evaluate expressions involving powers of $i$ Add and subtract complex numbers Multiply and divide complex numbers | Use exponential expressions to represent rational numbers Simplify/evaluate expressions involving positive and negative exponents and/or roots Simplify/evaluate expressions involving multiplying with exponents, powers of powers, and powers of products Simplify or evaluate expressions involving logarithms and exponents Factor algebraic expressions, including difference of squares and trinomials Simplify rational algebraic expressions | Write and/or solve quadratic equations (including factoring and using Quadratic Formula) Solve equations involving rational and radical expressions Write and/or solve a simple exponential or logarithmic equation Use algebra processes to solve a formula for a given variable Identify or describe the effect of changing parameters within a family of functions | Draw, identify, find, interpret, and/or write an equation and make predictions for a linear regression model for a scatter plot Use combinations, permutations, and the fundamental counting principle to solve problems involving probability Use odds to find probability and/or use probability to find odds Use probability for independent, dependent, or compound events to predict outcomes |

